

Present and Future Computing Requirements

# **Large-Scale Geophysical Imaging and Simulation**

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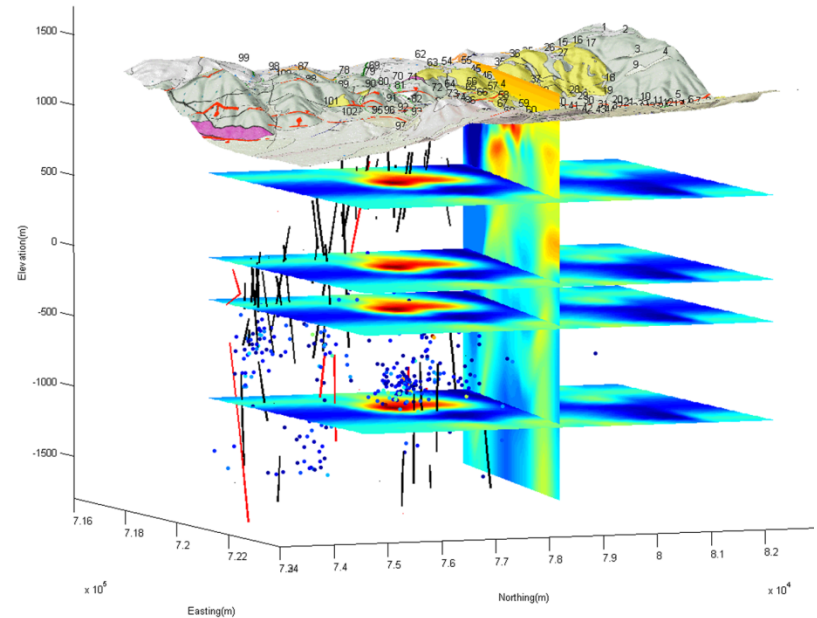
NERSC BES Requirements for 2017

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Gaithersburg, MD

# Why HPC => Time to Solution

- Why is this important?
  - More Science Can Get Done
  - More Breakthroughs
  - More Publications
  - More Realistic Models
  - More Understanding
  - End Member Simulations
  - Time Sensitive Decisions



# GEOFYSICAL IMAGING

- Seismic
  - 3D Reverse Time Migration
    - Large Scale Computations: 1,000s Cores, Weeks of Processing
  - 3D Elastic and Acoustic Full Waveform Inversion
    - Iterative reverse time migration
    - Promises Much Greater Image Fidelity
    - Formidable Numerical Issues – Local Minima, Very Good Starting Models Required
    - Frontier Research Area
    - Enormous Computation: 10,000's Cores, Months of Processing
- Electromagnetic (CSEM & MT)
  - 3D Full Waveform Inversion
    - Provides information on non-seismic attributes
    - Complements seismic imaging – through lower resolution
    - Constrained by seismic imaging
    - Computational demands also big: 1,000s to 10,000s cores
- Joint Seismic-Electromagnetic Imaging
  - The Holy Grail ?
    - Frontier Research Area
    - Grand Challenge Problem

# Wave Equations for Geophysical Simulation and Imaging

## Acoustic Waves

Time Domain

$$\left[ \frac{1}{v^2} \frac{\partial^2}{\partial t^2} - \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \right] p(x, y, z, t) = s(t).$$

Frequency Domain

$$\left[ \frac{\omega^2}{v^2} - \left( \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2} \right) \right] p(x, y, z, \omega) = s(\omega).$$

## Electromagnetic Waves

$$\nabla \times \nabla \times \mathbf{E}_s + i\omega\mu\sigma \mathbf{E}_s = \mathbf{S}.$$

Discretization Methods: Finite Differences, Finite Elements



# Elastic Wave Field Simulation

First- order system for velocity –stress components  
Laplace-Fourier Domain

$$s\rho v_x = \text{div}(\mathbf{\tau}_x) + f_x, \quad \mathbf{\tau}_x = (\tau_{xx}, \tau_{xy}, \tau_{xz});$$

$$s\rho v_y = \text{div}(\mathbf{\tau}_y) + f_y, \quad \mathbf{\tau}_y = (\tau_{xy}, \tau_{yy}, \tau_{yz});$$

$$s\rho v_z = \text{div}(\mathbf{\tau}_z) + f_z, \quad \mathbf{\tau}_z = (\tau_{xz}, \tau_{yz}, \tau_{zz});$$

$$s\tau_{xy} = \mu(\partial_y v_x + \partial_x v_y);$$

$$s\tau_{xz} = \mu(\partial_z v_x + \partial_x v_z);$$

$$s\tau_{yz} = \mu(\partial_z v_y + \partial_y v_z);$$

$$s\tau_{xx} = \lambda \text{div}(\mathbf{v}) + 2\mu \partial_x v_x;$$

$$s\tau_{yy} = \lambda \text{div}(\mathbf{v}) + 2\mu \partial_y v_y;$$

$$s\tau_{zz} = \lambda \text{div}(\mathbf{v}) + 2\mu \partial_z v_z.$$

$$\hat{\mathbf{M}} = \begin{pmatrix} M_{xx} & M_{xy} & M_{xz} \\ M_{xy} & M_{yy} & M_{yz} \\ M_{xz} & M_{yz} & M_{zz} \end{pmatrix}$$

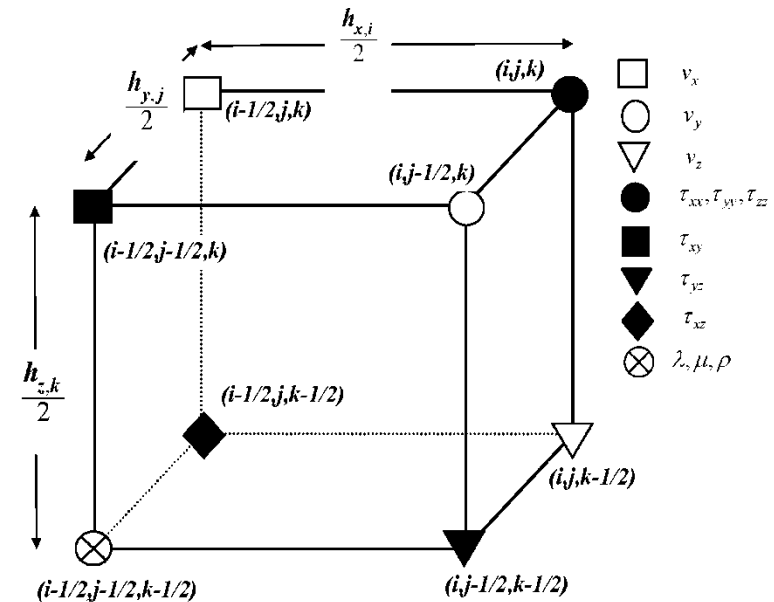
Forces  $f_{x,y,z}$  are defined via  $\nabla \cdot \hat{\mathbf{M}}$   
Moment-Tensor components (R. Graves 1996)

$v_{x,y,z}$  - velocity components,

$\tau_{xx,xy,xz,yz,yy,zz}$  - stress components,

$\rho$  - density,

$\lambda$  and  $\mu$  - Lamé coefficients.



# LARGE-SCALE MODELING & IMAGING CONSIDERATIONS

- Require Large-Scale Complex Modeling and Imaging Solutions
  - 10's of million's field unknowns (fwd problem; Maxwell's & Poisson's, acoustic and elastic field wave equations)
    - Solved with finite difference approximations & iterative Krylov solvers
  - Imaging grids 400 nodes on a side
    - Exploit gradient optimization & implicit Gauss-Newton schemes, adjoint state methods
- Parallel Implementation
  - Domain Decomposition Techniques, MPI Interconnect fabric
  - Two levels of parallelization
    - Model Space (simulation and inversion mesh)
    - Data Space (each transmitter/frequency - receiver set fwd calculation independent)
    - Installed & tested on multiple distributed computing systems; 10 – 30,000 Processors
- Above procedure satisfactory except for very largest problems
  - To treat such problems requires a higher level of efficiency
- Optimal Grids
  - Separate inversion grid from the simulation/modeling grid
  - Effect: A huge increase in computational efficiency ~ can be orders of magnitude

# HPC MODELING & INVERSE MODELING

- FURTHER CONSIDERATIONS
  - Sometimes Smaller Model Parameterizations Encountered
    - Induction logging, but still 1000' s of fwd solves needed for imaging
    - Stochastic imaging
- Parallel Implementation Considerations
  - Will the application scale with processors employed => 10' s to 10,000' s ?
    - Reduction in time to solution
    - Efficient exploitation of resources
    - Shows capability to attack large scale problems that cannot be solved otherwise

# Solver Selection

- Choice depends on problem:
  - Direct Solvers
    - Multiple Right Hand Side Solutions
    - Robust with Respect to Mesh Design
    - Requires Matrix Factorization – expensive and time consuming for large meshes
    - Parts of the solver solution inherently non-parallel (triangular forward and back solves)
    - Parallel Solvers: MUMPS, SUPER LU, PARDISO
  - Iterative Solvers
    - Single Right Hand Side Solution
    - Sensitive to Mesh Design – Preconditioning Required
    - Highly Efficient Solution Process for Large Meshes
    - Parallel Krylov Solvers: Your Own, PETSE and TRILINOS Libraries
    - Algebraic Multigrid and Preconditions



# Some HPC Applications

- Resistivity Mapping of Hydrocarbons
- End Member Solutions (SEAMS Resistivity Model)
- Geothermal Resource Evaluation
- Joint EM & Seismic Imaging
- 3D Elastic Wave-Field Simulation & Imaging

# Marine CSEM & MT Surveying

## CSEM

Deep-towed Electric Dipole transmitter

- ~ 100 Amps
- Water Depth 1 to 7 km
- Alternating current 0.01 to 3 Hz
- 'Flies' 50 m above the sea floor
- Profiles 10' s of km in length
- Excites vertical & horizontal currents
- Depth of interrogation ~ 3 to 4 km
- Sensitive to thin resistive beds

## MT

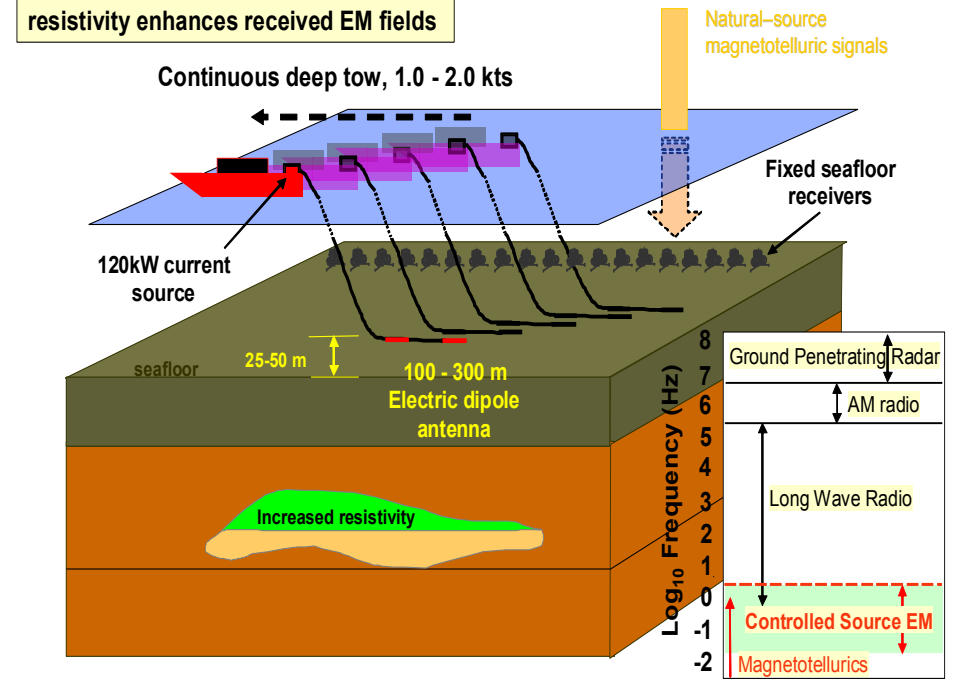
Natural Source Fields

- Less than 0.1 Hz
- Measured with CSEM detectors
- Sensitive to horizontal currents
- Depth of interrogation 10' s km
- Resolution is frequency dependent
- Sensitive to larger scale geology

### Marine EM Surveying

#### Basic Principle

Presence of increased subsurface resistivity enhances received EM fields



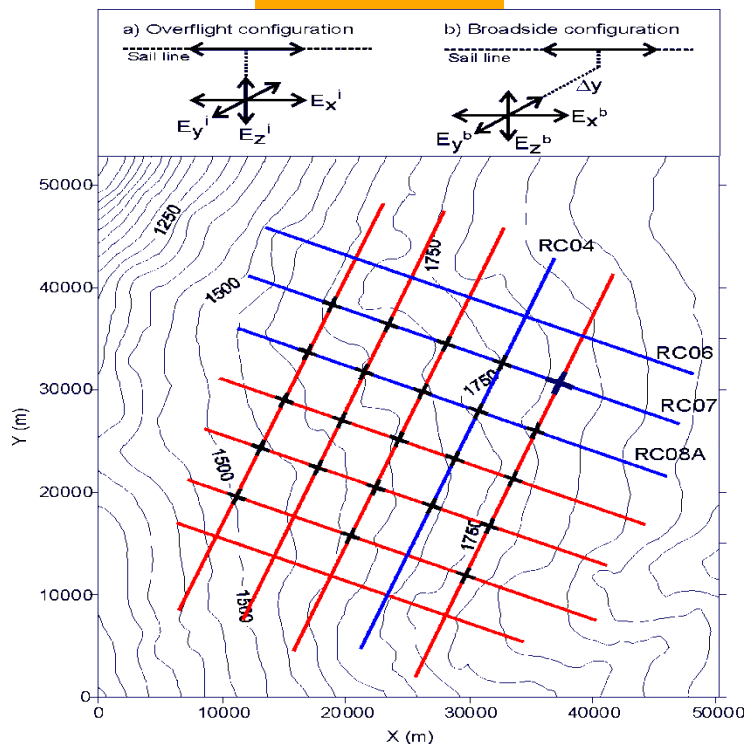
# Campos Basin CSEM Survey



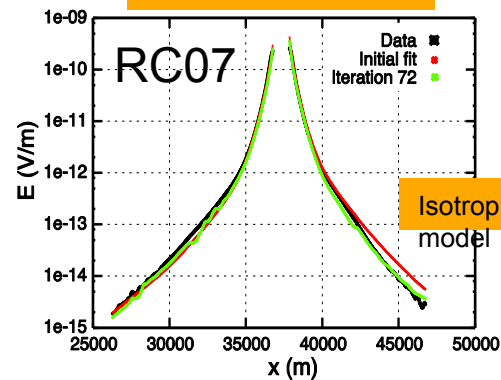
## Offshore Brazil

- Study: CSEM Imaging in the presence of electrical anisotropy
- Field Data: 23 detectors, 10 sail lines, 3 frequencies @ 1.25, 0.75, 1.25 Hz
- Image Processing: ~ 1 million data points, 27 million image cells
- Processing Times: 24 hours, 32,768 tasks, IBM Blue Gene (BG/L)
- Conclusions: data cannot be fit using isotropic model, anisotropic model required

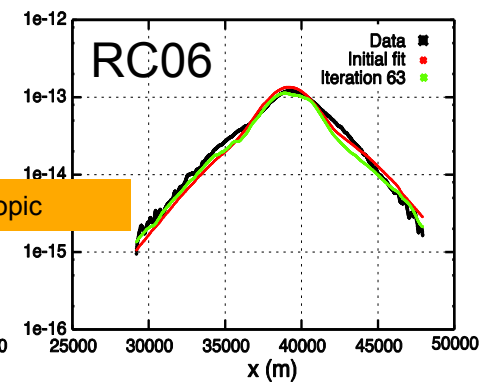
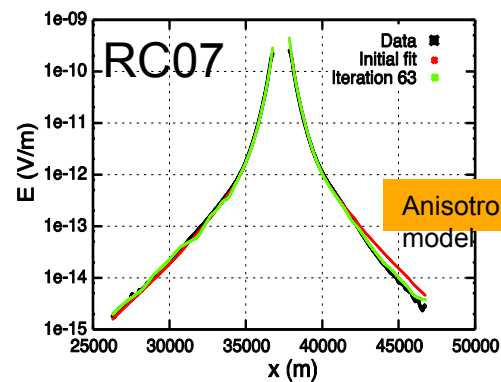
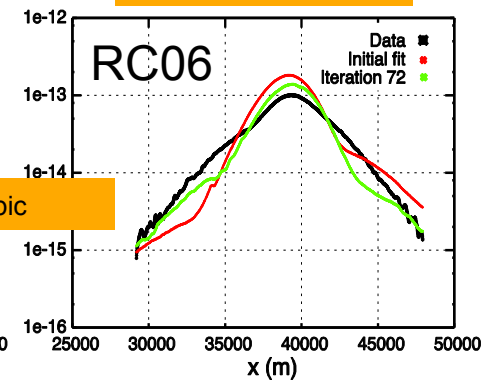
### Survey layout



### Overflight electric field

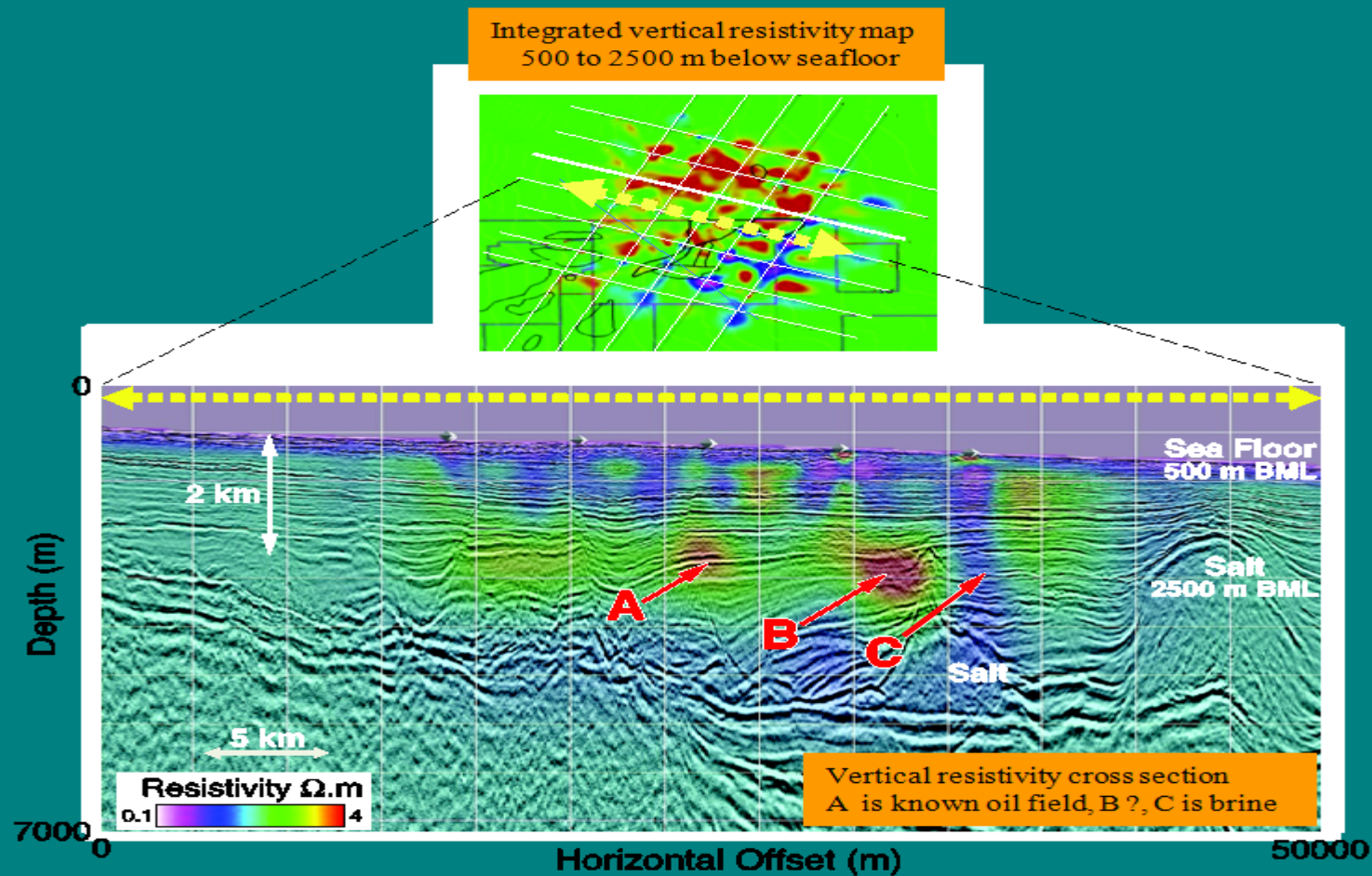


### Broadside electric field



# 3D CSEM Resistivity Imaging

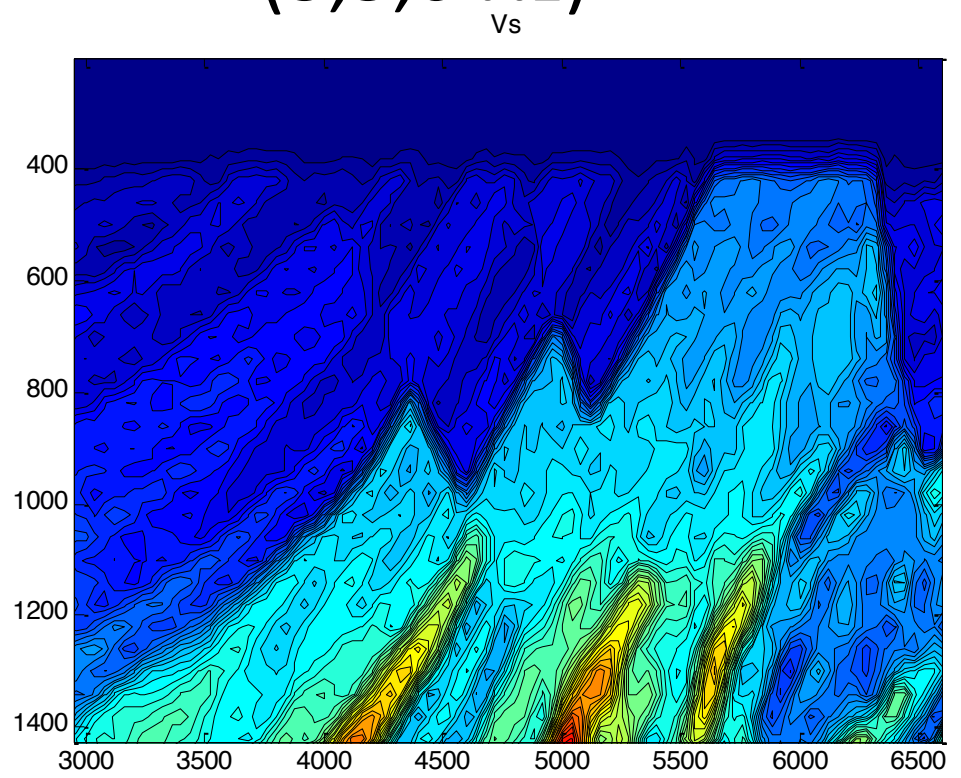
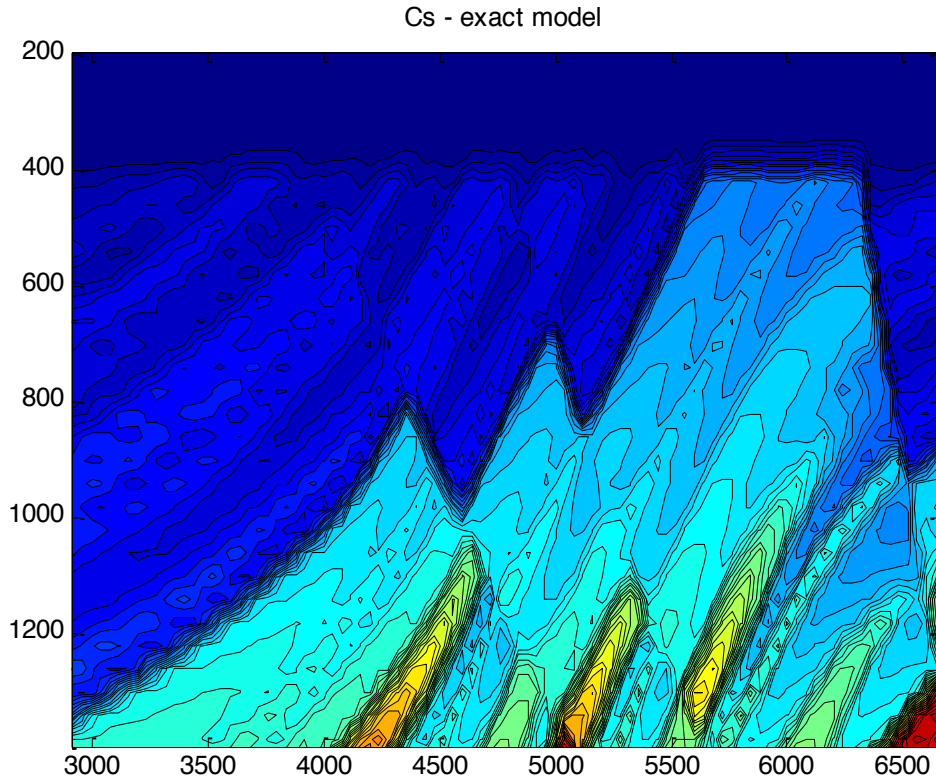
Offshore Brazil



# The Marmousi Model

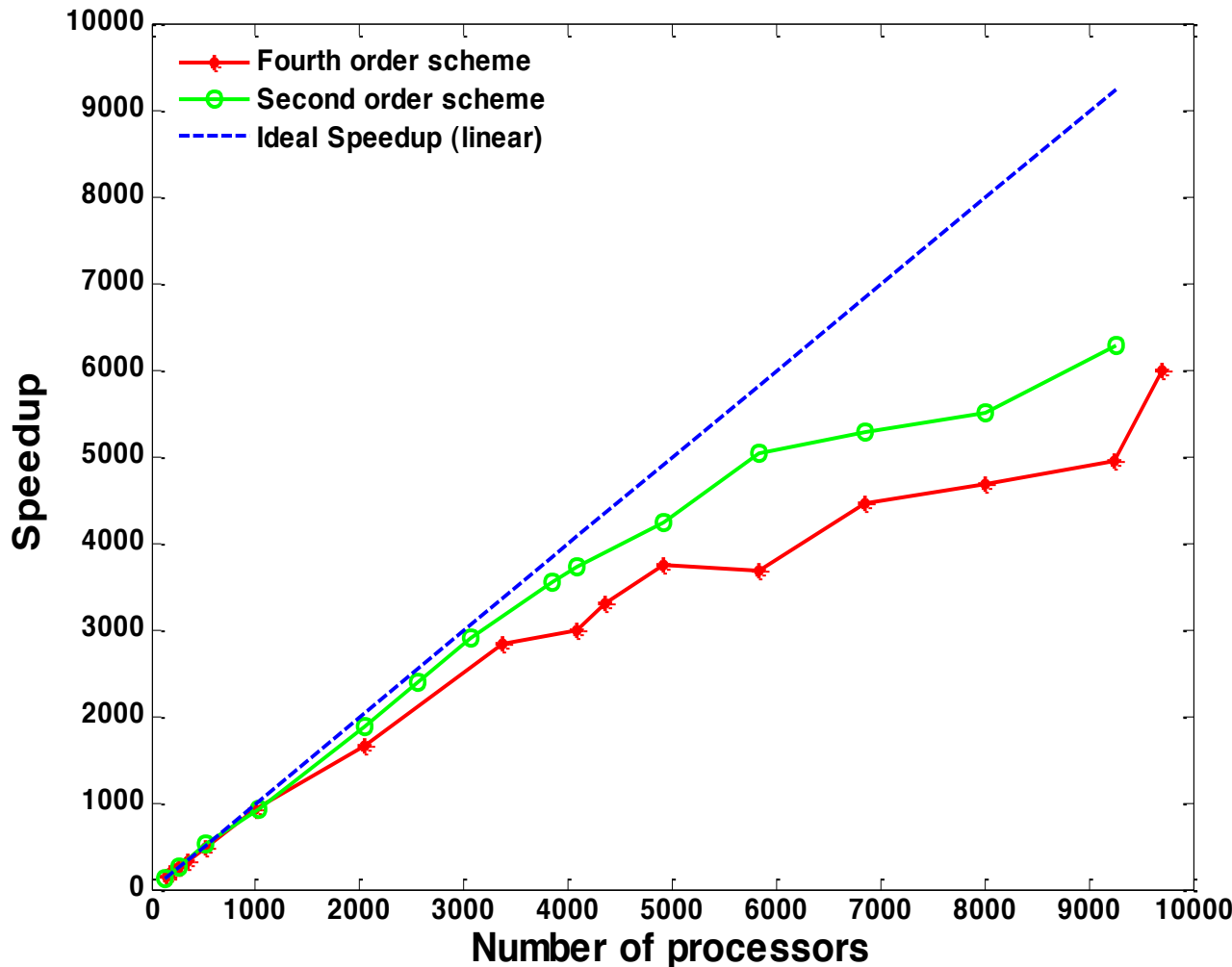
## Imaging results for shear velocity

- Exact model
- Inverted model (3,5,6 Hz)



# Measuring HPC Performance

## Parallel scaling of the Elastic simulator



### Speedup

$$S = \frac{T_1(n)}{T_p(n)} \leq p,$$

where  $p$  = “ideal speedup”,

$$T_1(n), T_p(n)$$

are the times for running a problem of size  $n$  on 1 and  $p$  processors

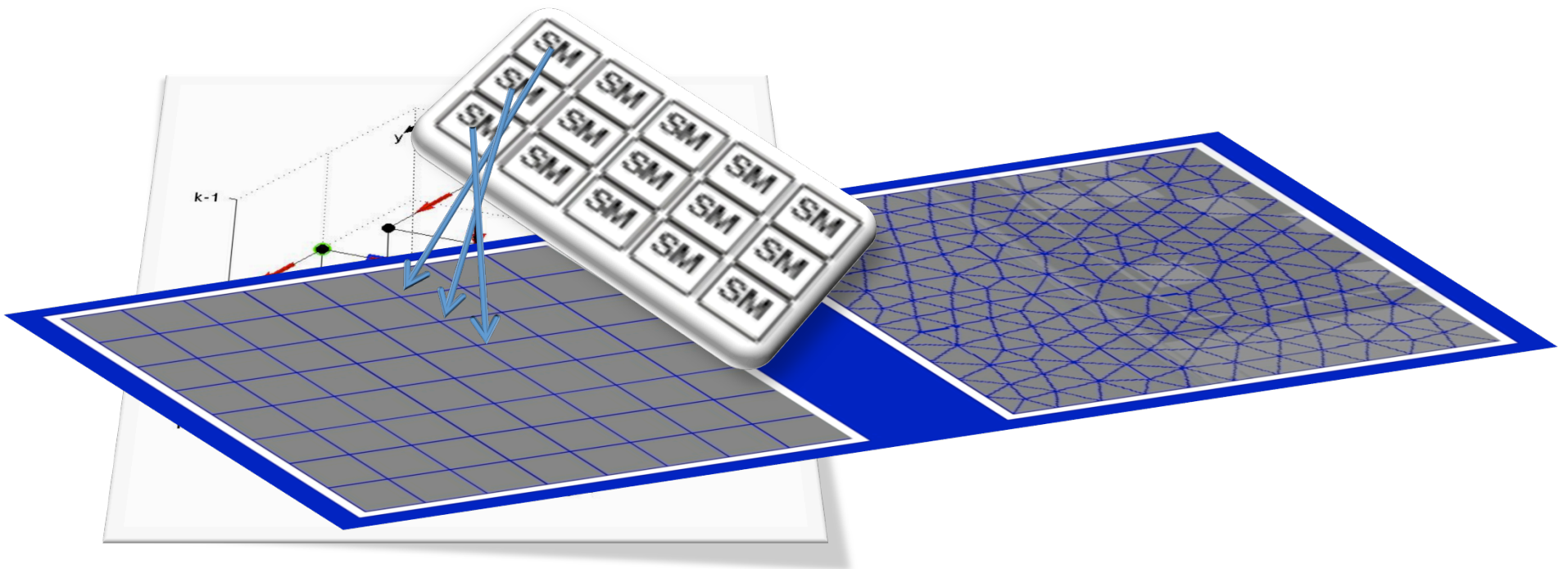
Scaling curves for a fixed-size (588x588x261) problem run on Cray XT4 – NERSC Franklin System



# Geophysical Simulations on GPUs

Main challenge:

Manage memory access in most efficient way



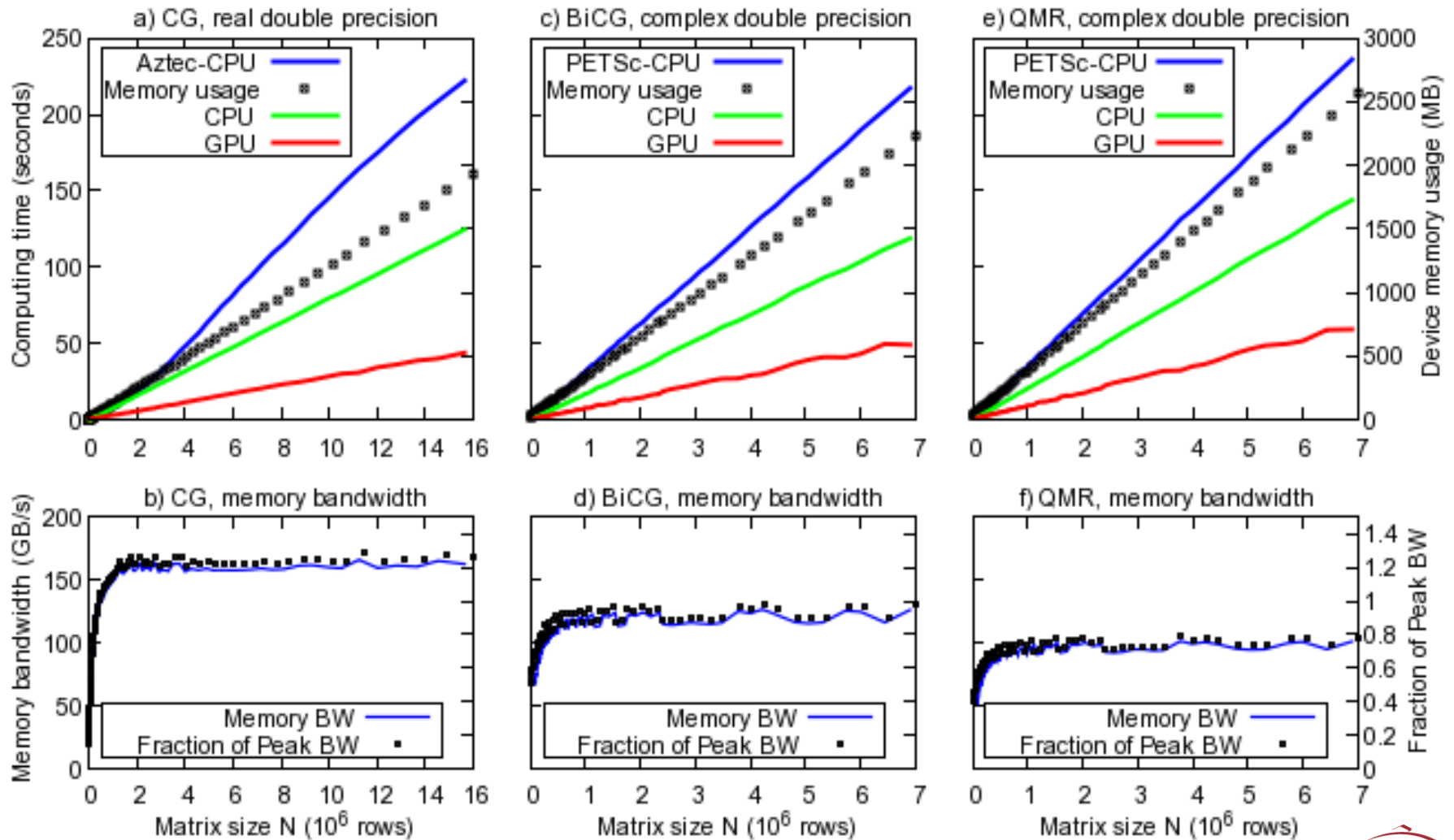
# Iterative Krylov Solver Performance Tests



**Typically used for EM problems:  
CG, BiCG, QMR**



# Computing times for 1000 Krylov solver iterations



# GPU/CPU-MPI Comparisons

- For Largest Problems Tested:
  - 1 GPU (448 processor cores)
    - Equivalent to 23 CPU' s for CG iteration (DC & IP Problems)
    - Equivalent to 19 QMR and BiCG iterations (EM and MT)
- GPU' s Impressive, but not good enough for now.
  - Marine CSEM and MT Imaging (Production)
    - Use routinely 64 to 512 CPU cores per fwd solve
    - What about multiple GPU' s with MPI (too slow for now)
  - Elastic Wave field modeling and Imaging
    - Similar performance comparisons are expected

## Current HPC Usage

- Machines currently using **Hopper and Edison at NERSC**
- Hours used in 2012-2013 is now approaching **16M**
- Biggest Jobs > **5000 to 20,000 compute cores**
- Run times per job **24 to 36 hours**
- Data read/written per run: **approximately 16 to 160 Gigabytes of data written to scratch mostly for for check pointing.**
- Maximum Memory used per (node **16 Gbytes** | core **0.5 Gbytes** | globally **2.5 to 5 Terrabytes**)
- Necessary software, services or infrastructure: **Fortran 90, 95, C, C++, MPI, Cuda**

# HPC Requirements for 2017

- Science goals: **solve problems approaching  $10^9$  grid nodes; elastic wave field simulation and imaging, joint imaging experiments, treat larger data volumes**
- Compute hours needed (in units of Hopper hours) **> 30M**
- Faster Solvers: **massively parallel algebraic Multigrid, designed Specifically from complex and complex-symmetric linear Systems.**
- Changes to memory needed per ( **2-4x** core | **2-4x** node | **2-4x** globally )
- Changes to necessary software, services or infrastructure: **hybrid computing systems are coming (multi-core GPU-CPU-MPI interconnects)**
- Legacy Software: **porting to such hybrid machines will be an issue**